



# A simplified physically-based breach model for a high concrete-faced rockfill dam: A case study

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## Abstract

A simplified physically-based model was developed to simulate the breaching process of the Gouhou concrete-faced rockfill dam (CFRD), which is the only breach case of a high CFRD in the world. Considering the dam height, a hydraulic method was chosen to simulate the initial scour position on the downstream slope, with the steepening of the downstream slope taken into account; a headcut erosion formula was adopted to simulate the backward erosion as well. The moment equilibrium method was utilized to calculate the ultimate length of a concrete slab under its self-weight and water loads. The calculated results of the Gouhou CFRD breach case show that the proposed model provides reasonable peak breach flow, final breach width, and failure time, with relative errors less than 15% as compared with the measured data. Sensitivity studies show that the outputs of the proposed model are more or less sensitive to different parameters. Three typical parametric models were compared with the proposed model, and the comparison demonstrates that the proposed physically-based breach model performs better and provides more detailed results than the parametric models.

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**Keywords:** Concrete-faced rockfill dam; Physically-based breach model; Parametric breach model; Sensitivity analysis; Gouhou CFRD

## 1. Introduction

The concrete-faced rockfill dam (CFRD) is a type of dam widely used throughout the world for different purposes, with sizes ranging from small irrigation projects to large reservoirs on major rivers. The CFRD design is considered to have a high degree of fundamental safety, especially against strong earthquake shaking, and to be appropriate for high dams (Li and Yang, 2012; Cen et al., 2016; Chen et al., 2016). It also has substantial advantages over the clay-core rockfill dam design (Sherard and Cooke, 1987), e.g., lower cost and easily

available materials. This has led to the selection of the CFRD design for very large reservoirs, for which low-level release facilities are neither feasible nor necessary (Sherard and Cooke, 1987; Modares and Quiroz, 2016; Gurbuz and Peker, 2016). At present, with the development and utilization of water resources, an array of high CFRDs with heights greater than 200 m are being built or planned in China (Chen, 2015; Zhou et al., 2015a; Du et al., 2015). These high dams and large reservoirs will bring tremendous financial benefits, but hidden safety issues should be given more attention (Zhou et al., 2015b; Jia et al., 2016; Yang et al., 2016; Niu et al., 2016). Although the CFRD has many advantages, there have also been some failure cases due to overtopping or seepage erosion (Wahl, 1998; Xu and Zhang, 2009; Xu, 2010). For several decades now, a series of physically-based breach models for earth dams have been put forward (ASCE/EWRI Task Committee on Dam/Levee Breaching, 2011; Chen, 2012; Xie et al., 2013; Zhong et al., 2016). Unfortunately,

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there have been few records made of CFRD breach modeling, except for some parametric models.

Investigation of CFRD failure cases around the world has revealed that only the Gouhou CFRD breach case in China has detailed records. Based on the survey data and model tests, the Gouhou CFRD breach may have begun with a piping failure. The subsequent breaching process can be delineated as follows: At first, a large amount of water leaked at the junction of a concrete slab and the bottom of a wave wall (Fig. 1). Then, the drained water scoured the downstream slope and caused sloughing. Under the effects of piping, scouring, and sloughing, the wave wall collapsed, and then overtopping dominated (Liu et al., 1998). Owing to the support of the concrete slab, the water head of overtopping flow increased slowly at the initial stage. With the erosion of dam materials, the breach crest diminished, and the length of the concrete slab suspended in air increased. The concrete slab broke off when it could no longer support the self-weight and water loads, and the discharge increased rapidly after the breaking of the concrete slab (Li, 1995; Chen et al., 2012). Then, the breach continued to deepen and widen until the remaining dam was stabilized under various loads.

In this study, based on the survey data and model tests of the Gouhou CFRD breach case, a simplified physically-based breach model for the Gouhou CFRD was developed. Considering the dam height, the initial scour position on the downstream slope was simulated using a hydraulic method. The broad-crested weir equation was used to simulate the breach flow discharge. The backward erosion was considered the key mechanism of breaching of compacted rockfill materials, which was reflected with a time-averaged headcut migration rate from an empirical formula of the energy method. The moment equilibrium method was adopted to simulate the ultimate length of the concrete slab.

## 2. Numerical model for Gouhou CFRD breach

### 2.1. Water balance equation

The water balance equation for the reservoir can be described as

$$\frac{dV}{dt} = A_s \frac{dz_s}{dt} = Q_{in} - Q_b - Q_{spill} - Q_{sluice} \quad (1)$$

where  $V$  is the volume of water in the reservoir,  $t$  is time,  $A_s$  is the surface area of the reservoir,  $z_s$  is the water surface elevation,  $Q_{in}$  is the inflow discharge,  $Q_b$  is the breach flow,  $Q_{spill}$  is the flow through spillways, and  $Q_{sluice}$  is the flow through sluice gates.

### 2.2. Breach flow

The overtopping flow at the breach can be calculated using the broad-crested weir equation:

$$Q_b = k_{sm} (c_1 B_b h^{1.5} + c_2 m h^{2.5}) \quad (2)$$

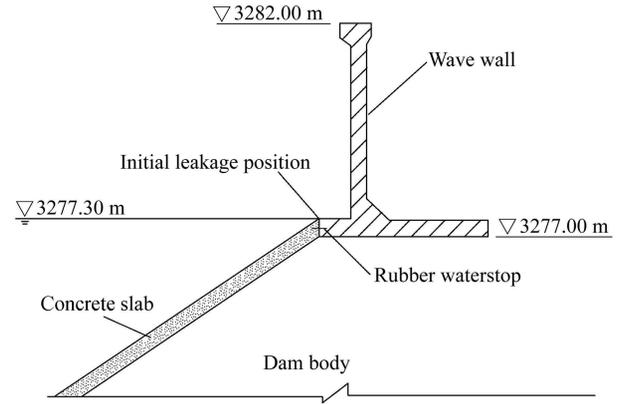


Fig. 1. Initial leakage position of Gouhou CFRD.

where  $B_b$  is the breach bottom width;  $h = z_s - z_b$ , where  $z_b$  is the elevation of the breach bottom;  $m$  is the slope of the breach;  $c_1 = 1.7$ ;  $c_2 = 1.3$ ; and  $k_{sm}$  is the submergence correction for tailwater effects on weir outflow.

### 2.3. Initial scour position

Visser (1998) pointed out that, on account of the steepness of the downstream slope of the dam, flow accelerates from point  $F$  at the top of the downstream slope to point  $P$  on the downstream slope, where the normal flow velocity is reached if the slope is long enough (Fig. 2). Beyond point  $P$ , breach flow remains uniform with its velocity and water depth being normal values, and it is defined as the initial scour position. The distance  $l_n$  between  $F$  and  $P$  can be approximated with the following expression:

$$l_n = \frac{2.5(Fr_n^2 - 1)d_n}{\tan \beta} \quad (3)$$

where  $\beta$  is the inclination angle of the downstream slope,  $d_n$  is the normal water depth, and  $Fr_n$  is the Froude number at point  $P$ .  $Fr_n$  is calculated as follows:

$$Fr_n^2 = \frac{U_n^2 B_{tm}}{g d_n B_n \cos \beta} \quad (4)$$

where  $U_n$  is the cross-sectional averaged normal flow velocity,  $B_{tm}$  is the breach width at the dam crest under the normal flow conditions,  $B_n$  is the breach width at the downstream slope, and  $g$  is the gravitational acceleration.

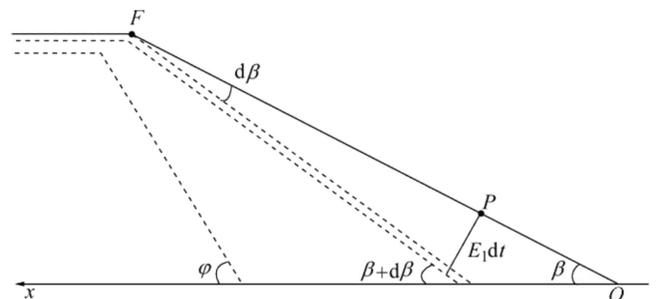


Fig. 2. Lowering of dam crest and steepening of downstream slope.

$U_n$  and  $d_n$  beyond point  $P$  are calculated, respectively, as

$$U_n = C\sqrt{R_n \sin \beta} \quad (5)$$

$$d_n = \frac{Q_b}{U_n B_n} \quad (6)$$

where  $R_n$  is the hydraulic radius of breach under the normal flow conditions, and  $C$  is the Chezy coefficient.

#### 2.4. Breach development

At the initial stage of dam breaching, the breach flow velocity at the dam crest is relatively small compared with that of the downstream slope. Due to the larger erosion rate at point  $P$  than at the upper part of the downstream slope, the slope becomes steeper as the breach develops, and, accordingly, the slope angle increases from an initial value  $\beta$  at  $t = t_0$  to a critical value  $\varphi$  at  $t = t_1$ , which is assumed to be the internal friction angle of rockfill materials (Fig. 2).

A shear stress equation is used to describe the erosion rate of soil (USDA-NRCS, 1997):

$$E = k_d(\tau_b - \tau_c) \quad (7)$$

where  $E$  is the erosion rate,  $k_d$  is the erodibility coefficient,  $\tau_b$  is the bed shear stress, and  $\tau_c$  is the critical shear stress determined using the Shields diagram.

The coefficient  $k_d$  is usually calculated with the empirical formula proposed by Temple and Hanson (1994):

$$k_d = \frac{10\rho_w}{\rho_d} \exp \left[ -0.121c^{0.406} \left( \frac{\rho_d}{\rho_w} \right)^{3.1} \right] \quad (8)$$

where  $\rho_w$  is the density of water,  $\rho_d$  is the dry density of soil, and  $c$  is the clay ratio.

The bed shear stress is determined by the Manning equation:

$$\tau_b = \frac{\rho_w g n^2 Q_b^2}{A^2 R^{1/3}} \quad (9)$$

where  $A$  is the flow area, and  $R$  is the hydraulic radius. The Manning's roughness coefficient  $n$  is related to sediment median size  $d_{50}$  (m) as follows:

$$n = \frac{d_{50}^{1/6}}{M_n} \quad (10)$$

where  $M_n$  is an empirical coefficient, and  $M_n = 12$  for the field cases in this study (Wu, 2013).

Eq. (7) can be used to describe the erosion at the dam crest  $dz_b/dt$ . With regard to the erosion on the downstream slope, the equation for the increment  $d\beta$  can be expressed as

$$d\beta = \frac{(E_1 - E_0/\cos \beta)dt}{l_n} \quad (11)$$

where  $E_1$  is the erosion rate at the initial scour position on the downstream slope, and  $E_0$  is the erosion rate at the top of the downstream slope.

When the downstream slope angle reaches the internal friction angle  $\varphi$ , it is assumed that the slope angle maintains a constant value. Then, a formula of the time-averaged migration rate is utilized to reflect the backward erosion (Temple, 1992):

$$\frac{dx}{dt} = C_T q^{1/3} H_c^{1/2} \quad (12)$$

where  $dx/dt$  is the backward erosion rate,  $C_T$  is the backward erosion coefficient,  $q$  is the discharge per unit width, and  $H_c$  is the overfall height.

When a breach occurs along the dam axis (Fig. 3), the relationship between horizontal expansion and vertical undercutting is determined by

$$\Delta B_t = \frac{n_{loc} \Delta z_b}{\sin \varphi} \quad (13)$$

$$\Delta B_b = n_{loc} \Delta z_b \left( \frac{1}{\sin \varphi} - \frac{1}{\tan \varphi} \right) \quad (14)$$

where  $B_t$  is the breach top width;  $\Delta B_t$  and  $\Delta B_b$  are the horizontal expansion values of breach at the breach top and breach bottom for each time step, respectively;  $n_{loc}$  is the indicator of breach location, with  $n_{loc} = 1$  for a breach located on a side of the dam, and  $n_{loc} = 2$  for a breach located at the middle of dam length (Wu, 2013); and  $\Delta z_b$  is the vertical undercutting value for each time step. In this study, because the dam was made of rockfill materials, the breach slope angle was assumed to be the same as the internal friction angle.

#### 2.5. Failure of concrete slab

Owing to the supporting function, the concrete slabs retain water. The initial breach deepens and widens under the erosion by the overflow water. With the erosion of downstream rockfill materials, the breach crest decreases gradually, and the length of suspended concrete slabs increases. The concrete slabs break off when they cannot sustain the self-weight and water loads.

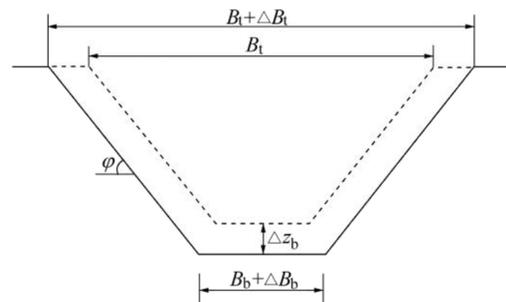


Fig. 3. Breach development along dam axis.

In this study, the moment equilibrium method was utilized to analyze the stability of each concrete slab. In order to simplify the analysis, the concrete slab was assumed to be a cantilever slab when the supporting sand gravel vanished. The self weight-induced bending moment can be calculated as follows:

$$M_1 = \frac{\rho_m g m_1 \delta w L_d^2}{2\sqrt{1+m_1^2}} \quad (15)$$

where  $\rho_m$  is the density of the concrete slab,  $m_1$  is the upstream slope,  $\delta$  is the thickness of the concrete slab,  $w$  is the width of the concrete slab, and  $L_d$  is the length of the damaged concrete slab.

The water load-induced bending moment is

$$M_2 = \frac{\rho_w g (z_s - z_f) w L_d^2}{2} + \frac{\rho_w g w L_d^3}{6\sqrt{1+m_1^2}} \quad (16)$$

where  $z_f$  is the crest elevation of the concrete slab.

The total bending moment of the concrete slab is

$$M = M_1 + M_2 = \frac{\rho_m g m_1 \delta w L_d^2}{2\sqrt{1+m_1^2}} + \frac{\rho_w g (z_s - z_f) w L_d^2}{2} + \frac{\rho_w g w L_d^3}{6\sqrt{1+m_1^2}} \quad (17)$$

The ultimate bending moment of the concrete slab can be calculated according to the *Design Code for Hydraulic Concrete Structures* (SL191–2008):

$$M_u = f_y A_c \left( h_0 - 0.5 \frac{f_y A_c}{f_c w} \right) \quad (18)$$

where  $f_y$  is the design value of rebar's tensile strength;  $A_c$  is the cross-sectional area of rebar in the tensile region;  $h_0$  is the distance from the barycenter of the tensile rebar to the edge of the compressive zone; and  $f_c$  is the design value of concrete axial compressive strength. Thus,  $L_d$  can be determined by

$$\frac{\rho_m g m_1 \delta w L_d^2}{2\sqrt{1+m_1^2}} + \frac{\rho_w g (z_s - z_f) w L_d^2}{2} + \frac{\rho_w g w L_d^3}{6\sqrt{1+m_1^2}} = f_y A_c \left( h_0 - 0.5 \frac{f_y A_c}{f_c w} \right) \quad (19)$$

### 3. Case study

#### 3.1. Calculated parameters

The Gouhou CFRD breach case, with detailed measurement data, was chosen as the representative case study. The Gouhou CFRD has a maximum height of 71.0 m and a total storage of

Table 1  
Parameters of Gouhou CFRD.

$\rho_d$ (kg/m <sup>3</sup> )	$w$ (m)	$\delta$ (m)	$f_y$ (N/m <sup>2</sup> )	$h_0$ (m)	$f_c$ (N/m <sup>2</sup> )	$A_c$ (m <sup>2</sup> )	$\rho_m$ (kg/m <sup>3</sup> )
2090.0	14.0	0.35	$3.0 \times 10^8$	0.175	$9.6 \times 10^6$	0.018	2600.0

3.3 million m<sup>3</sup>. Because the failure time of the Gouhou CFRD was only 2.33 h, it was assumed that there was no inflow during dam breaching. The crest length ( $L$ ) and width ( $B$ ) of the dam were 265.0 m and 7.0 m, respectively. The upstream slope ( $m_1$ ) and downstream slope ( $m_2$ ) were 0.625 and 0.667, respectively. The concrete slab crest elevation was 3277.00 m. The initial water level elevation was set at 3277.30 m. The data used in the present study were selected from Xu and Zhang (2009), as well as several laboratory experiments and field investigations (Li, 1995; Liu et al., 1998; Li and Sheng, 2000). The initial breach depth and width were both 5.0 m. The median size ( $d_{50}$ ) of the materials was determined to be 15.0 mm, an average value obtained from the typical grain composition curves of the Gouhou CFRD (Li and Sheng, 2000); the Manning's roughness coefficient ( $n$ ) was calculated as 0.041 using Eq. (10); the cohesion and internal friction angle of soil were determined to be 60 kPa and 40°, respectively, from the results of large-scale tri-axial tests (Li and Sheng, 2000); the clay ratio was assumed to be 0; and the erodibility coefficient ( $k_d$ ) was estimated to be 5.66 cm<sup>3</sup>/(N·s) using Eq. (8). Based on the experimental data and those from Robinson (1996), Bennett et al. (2000), and Mei et al. (2016), the backward erosion coefficient ( $C_T$ ) was assumed to be 0.015 m<sup>-1/6</sup>·s<sup>-2/3</sup>. Other parameters related to reservoir characteristics and soil properties of the Gouhou CFRD are listed in Table 1.

Fig. 4 shows the layout of the concrete slabs of the Gouhou CFRD, and the damaged slabs are denoted with numbers. According to the field investigation, the slab failure occurred at the center of the dam.

#### 3.2. Calculated results

In this study, the simulation of Gouhou CFRD breaching started at the occurrence of wave wall collapse. The overtopping flow then eroded the downstream slope. The calculated results of peak breach flow ( $Q_p$ ), final breach top width ( $B_{if}$ ), final breach bottom width ( $B_{bf}$ ), time of the peak breach flow ( $t_p$ ), and failure time ( $t_f$ ), as well as the measured data from Xu and Zhang (2009), are shown in Table 2, where  $t_f$  is the time period from the beginning of dam breaching to the

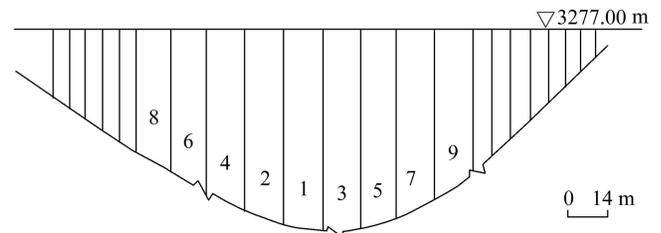


Fig. 4. Layout of concrete slabs of Gouhou CFRD.

Table 2  
Results of Gouhou CFRD breach case.

Method	$Q_p$ (m <sup>3</sup> /s)	$B_{if}$ (m)	$B_{bf}$ (m)	$t_p$ (h)	$t_f$ (h)
Measured	2050.0	138.0	61.0		2.33
Calculated	2152.2	143.6	67.5	0.65	2.67

moment when 99% of the final breach width is reached. Figs. 5 and 6 show the calculated breach flow hydrograph and the breach width development.

The calculated results show that, with the erosion of dam materials, the concrete slabs broke off, and the length of the first damaged concrete slab was 7.4 m at 0.50 h after dam breaching; then, the breach flow discharge increased immediately, and the peak breach flow, which was 5.0% larger than the measured data, occurred at 0.65 h after dam breaching. Likewise, the final breach top and bottom widths of the calculated results were 4.1% and 10.7% larger than the measured data, respectively; for the failure time, the calculated result was 14.6% longer than the measured one. Overall, the proposed model gives reasonable results, with relative errors less than 15.0%.

### 3.3. Sensitivity analysis

Sensitivity analysis of model parameters was conducted in this study. The erodibility coefficient and the backward erosion coefficient are the key parameters, and they are highly empirical with significant uncertainties. Owing to the wide grading of the CFRD materials, the grain size should be taken into account. Thus, the influences of the three parameters on the calculated breach characteristics were assessed for the proposed model. In the parameter sensitivity analysis,  $k_d$  and  $C_T$  were multiplied by 0.5 and 2.0, respectively, and  $d_{50}$  was chosen from the top and bottom boundary lines, which were 3 mm and 500 mm, respectively. In addition, the effects of the geometry of the dam (e.g., the crest length and the upstream and downstream slopes) and the internal friction angle were also taken into account. Considering the final top breach width in Table 2, the crest length of the dam was assumed to be 100.0 m and 530.0 m, respectively. Using actual CFRDs as references, the upstream and downstream slopes were set as 0.556 and 0.714 for sensitivity analysis, respectively. For the internal friction angle, the values were assumed to be  $30^\circ$  and  $50^\circ$ , respectively. The calculated  $Q_p$ ,  $B_{tf}$ ,  $B_{bf}$ , and  $t_p$  regarding the varied parameters are shown in Table 3. The changes of these quantities in percentage as compared with the calculated data in Table 2 are also given.

Table 3 shows that the peak breach flow is most sensitive to the erodibility coefficient and least sensitive to the internal

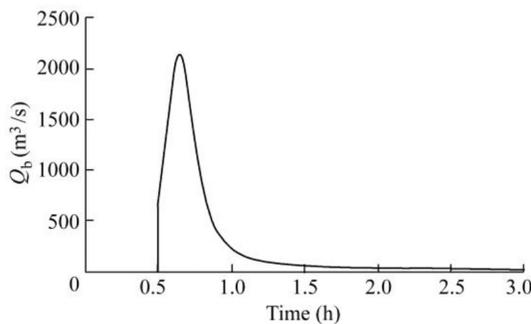


Fig. 5. Breach flow hydrograph.

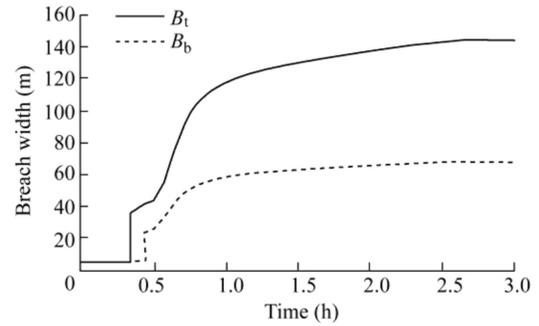


Fig. 6. Breach width development.

friction angle, the final breach top and bottom widths are both most sensitive to the soil erodibility coefficient and least sensitive to the upstream and downstream slopes, and the time of peak breach flow is most sensitive to the backward erosion coefficient and least sensitive to the crest length of the dam.

### 3.4. Comparison with parametric breach models

Owing to the lack of relevant physically-based models, the proposed breach model was compared with three parametric breach models with regard to the calculation of the peak breach flow, final average breach width, and failure time of dam breaching: the USBR (1988), Froehlich (1995a, 1995b), and Xu and Zhang (2009) models. The USBR (1988) model is as follows:

$$Q_p = 19.1H_w^{1.85} \quad (20)$$

$$B_{ave} = 3H_w \quad (21)$$

$$t_f = 0.011B_{ave} \quad (22)$$

where  $H_w$  is the depth of water above the breach invert at the failure time, and  $B_{ave}$  is the final average breach width.

The Froehlich (1995a, 1995b) model considers the overtopping and piping using a coefficient  $K_0$ . The formulas are as follows:

$$Q_p = 0.607V_w^{0.295}H_w^{1.24} \quad (23)$$

$$B_{ave} = 0.1803K_0V_w^{0.32}H_b^{0.19} \quad (24)$$

$$t_f = 0.0025V_w^{0.53}H_b^{-0.9} \quad (25)$$

where  $V_w$  is the volume of water above the breach invert,  $H_b$  is the breach depth, and  $K_0$  is 1.4 for overtopping and 1.0 for piping.

The Xu and Zhang (2009) model considers more factors, such as the dam type, erodibility, failure mode, and so on. The formulas are as follows:

$$\frac{Q_p}{\sqrt{gV_w^{5/3}}} = 0.175 \left( \frac{H_d}{H_r} \right)^{0.199} \left( \frac{V_w^{1/3}}{H_w} \right)^{-1.274} e^{B_4} \quad (26)$$

Table 3  
Sensitivity analysis results for different parameters.

Analyzed parameter	$Q_p$ (m <sup>3</sup> /s)	Variation of $Q_p$ (%)	$B_{tr}$ (m)	Variation of $B_{tr}$ (%)	$B_{br}$ (m)	Variation of $B_{br}$ (%)	$t_p$ (h)	Variation of $t_p$ (%)
$0.5k_d$	853.3	-60.4	117.9	-17.9	58.5	-13.3	0.78	+20.0
$2.0k_d$	3775.1	+75.4	189.6	+32.0	89.7	+32.9	0.58	-10.8
$0.5C_T$	2015.7	-6.3	129.9	-9.5	59.8	-11.4	1.12	+72.3
$2.0C_T$	2235.6	+3.9	156.7	+9.1	73.4	+8.7	0.38	-41.5
$d_{50} = 3.0$ mm	2103.2	-2.3	134.1	-6.6	62.7	-7.1	0.57	-12.3
$d_{50} = 500.0$ mm	3594.4	+67.0	150.1	+4.5	71.5	+5.9	2.16	+232.3
$L = 100.0$ m	1754.0	-18.5	100.0	-30.4	60.3	-10.7	0.65	0
$L = 503.0$ m	2152.2	0	143.6	0	67.5	0	0.65	0
$m_1 = m_2 = 0.556$	1925.7	-10.5	147.4	+2.7	69.7	+3.3	0.84	+29.2
$m_1 = m_2 = 0.714$	2408.4	+11.9	143.6	-2.7	65.3	-3.3	0.63	-3.1
$\varphi = 30^\circ$	2139.7	-0.6	152.9	+6.5	63.4	-6.1	0.66	+1.5
$\varphi = 50^\circ$	2154.7	+0.1	138.5	-3.6	71.3	+5.6	0.64	-1.5

$$\frac{B_{ave}}{H_b} = 0.787 \left(\frac{H_d}{H_r}\right)^{0.133} \left(\frac{V_w^{1/3}}{H_w}\right)^{0.652} e^{B_3} \tag{27}$$

$$\frac{t_f}{t_r} = 0.304 \left(\frac{H_d}{H_r}\right)^{0.707} \left(\frac{V_w^{1/3}}{H_w}\right)^{0.1228} e^{B_5} \tag{28}$$

where  $H_d$  is the dam height,  $H_r$  is a reference dam height set as 15 m, and  $t_r$  is a reference failure time set as 1 h. The coefficient  $B_3 = b_3 + b_4 + b_5$ , where  $b_3 = -0.041, 0.026$ , and  $0.226$  for dams with core walls, concrete-faced dams, and homogeneous/zoned-fill dams, respectively;  $b_4 = 0.389$  for piping; and  $b_5 = 0.291, 0.140$ , and  $0.391$  for high, medium, and low dam erodibility, respectively. The coefficient  $B_4 = b_3 + b_4 + b_5$ , where  $b_3 = -0.503, -0.591$ , and  $-0.649$  for dams with core walls, concrete-faced dams, and homogeneous/zoned-fill dams, respectively;  $b_4 = -1.039$  for piping; and  $b_5 = -0.007, -0.375$ , and  $-1.362$  for high, medium, and low dam erodibility, respectively. The coefficient  $B_5 = b_3 + b_4 + b_5$ , where  $b_3 = -0.327, -0.674$ , and  $-0.189$  for dams with core walls, concrete-faced dams, and homogeneous/zoned-fill dams, respectively;  $b_4 = -0.611$  for piping; and  $b_5 = -1.205, -0.564$ , and  $0.579$  for high, medium, and low dam erodibility, respectively.

The formulas from USBR (1982, 1988), Froehlich (1995a, 1995b), and Xu and Zhang (2009) represent three generations of parametric breach models obtained by regressions of single to multiple variables. The Gouhou CFRD was considered to have low erodibility and categorized to be piping failure in the models above because the dam breach initiated with the

seepage erosion.  $H_d, H_b, H_w$ , and  $V_w$  were determined to be 71.0 m, 48.0 m, 44.0 m, and  $3.18 \times 10^6$  m<sup>3</sup>, respectively, according to the conditions of the dam breach case.

Table 4 gives the results of the three parametric breach models and the proposed physically-based breach model, as well as their comparison with the measured data. Of the three models, the Xu and Zhang (2009) formulas perform best, followed by the Froehlich (1995a, 1995b) formulas and the USBR (1982, 1988) formulas. This is understandable because the Xu and Zhang (2009) formulas consider more factors and are based on larger databases.

Table 4 also shows that the proposed physically-based breach model performs significantly better than the three parametric breach models. In addition, a simplified physically-based breach model can give more detailed results, such as the breach hydrograph and breach development process shown in Figs. 5 and 6, than a parametric model.

#### 4. Conclusions

A simplified physically-based breach model for high CFRDs was developed, and the Gouhou CFRD breach case, with detailed measured data, was chosen to test the proposed model. The calculated results show that the proposed model gives reasonable values for the peak breach flow, final breach width, and failure time, with relative errors less than 15%. Sensitivity studies show that the peak breach flow is most sensitive to soil erodibility and least sensitive to the internal friction angle, the final breach top and bottom widths are both most sensitive to soil erodibility and least sensitive to the upstream and downstream slopes, and the failure time is most sensitive to the backward erosion coefficient and least sensitive to the dam crest length. In addition, the proposed breach model was compared with three typical parametric breach models. The comparison shows that the proposed physically-based breach model performs better and provides more detailed results than the parametric models. The proposed model adopts an alternative method to describe the characteristics of widely graded soil materials, and further studies and tests are needed to validate and improve the proposed breach model.

Table 4  
Results of parametric breach models and proposed physically-based breach model for Gouhou CFRD breach case.

Data source	$Q_p$ (m <sup>3</sup> /s)	Error of $Q_p$ (%)	Error of $B_{ave}$ (m)	Error of $B_{ave}$ (%)	Error of $t_f$ (h)	Error of $t_f$ (%)
Measured data	2050.0		99.5		2.33	
USBR (1982,1988)	20961.4	+922.5	132.0	+32.7	1.45	-37.8
Froehlich (1995a, 1995b)	5486.4	+167.6	45.3	-54.5	0.22	-90.6
Xu and Zhang (2009)	2113.0	+3.1	48.0	-51.8	1.98	-15.0
Proposed model	2152.2	+5.0	105.6	+6.0	2.67	+14.6

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